

Testing soft electroweak supersymmetry breaking from neutralino, chargino, and charged Higgs boson pair production at linear colliders

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We consider the production of neutralino, chargino, and charged Higgs boson pairs in the Minimal Supersymmetric Standard Model (MSSM) framework at future e^+e^- colliders. We show that, for c.m. energies in the 1 TeV range and in a moderately light supersymmetry (SUSY) scenario, a combined analysis of the slopes of these production cross sections could lead to a strong consistency test involving the soft supersymmetric breaking parameters M_1 , M_2 , the Higgsino parameter μ , and $\tan\beta$.

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It is a widespread hope within the members of the high energy elementary particle physics community that the upcoming experiments at Tevatron [1] and at LHC [2] will finally reveal the existence of supersymmetric particles, via direct production of sparticle-antiparticle pairs. In such an exciting hypothesis, the simplest available theoretical supersymmetric model, the Minimal Supersymmetric Standard Model (MSSM), will acquire the same role that belonged to the standard model (SM) after the W, Z discoveries, and a long and crucial period of precision tests will start, aiming to confirm, or to disprove, the main theoretical assumptions that were used in the practical construction of the model.

For the MSSM case, this program requires the construction of a linear e^+e^- collider [3] that explores the c.m. TeV energy region. This machine should be sufficiently accurate to provide the same kind of consistency tests of the model that were achieved in the hundred GeV region at LEP for the standard model, from detailed analyses of several independent one-loop virtual effects.

If such an ambitious project is to be carried on, a clean investigation strategy will undoubtedly be welcome, given the fact that the involved theoretical model has a not simple structure in which several independent parameters are implied. As a consequence of this feature, it might be appreciable to identify clean experimental measurements that possibly isolate in a relatively simple way a reduced subset of parameters and of theoretical assumptions behind them.

The aim of this short paper is to show that a dedicated combined analysis of the process of production of neutralino, chargino, and charged Higgs boson pairs might lead to a relevant precision test of the theoretical assumptions that were used to fix not only the basic supersymmetric sector, (i.e. the chiral superpotential and the gauge multiplet), but also the gaugino component of the soft supersymmetry breaking of the model. This will be done

in the paper by assuming a scenario of “moderately” light SUSY particles (i.e. the various masses are all below, roughly, 350 GeV) and a c.m. energy $\sqrt{s}$ in the one TeV region. Under these two assumptions, a simple asymptotic expansion of so-called “Sudakov type” is effective [4]. But the approach would not change for larger SUSY masses <700 GeV since a related c.m. energy rescaling would still be possible, from our previous experience, up to $\sqrt{s}$ values of about 2 TeV, where the resummation to higher orders is still not necessary [4].

After this brief description of the strategy of our approach, we are now ready to illustrate the practical details of our work. With this aim, we must recall, for the reader's convenience, that the relevant details of an analogous procedure, limited to the combination of chargino and charged Higgs pairs production, have already appeared in a previous paper [5]. It was shown there that from the combined analyses of the slopes of the total cross sections in a c.m. energy range of about 1 TeV, assuming a “light” SUSY scenario where all the relevant sparticle masses lie below $\sim 350\text{--}400$ GeV, a strong constraint on $\tan\beta$ (mostly produced by the Higgs cross section), and a strip in the (M_2, μ) plane (only produced by the chargino cross sections) were derivable. Here M_2 is the soft SUSY breaking wino mass, μ is the Higgsino mass parameter, and $\tan\beta = v_2/v_1$ is the ratio of the two Higgs doublets vacuum expectation values (VEVs). The novel process that we consider in this paper is neutralino pair production, and we shall show that its addition to the other processes will lead to highly improved constraints on the previous parameters, with the additional presence of M_1 , the soft SUSY breaking bino mass. With this aim, we now briefly list the relevant theoretical formulas that we need for the analysis.

At the Born level, the neutralino pair production process $e^+e^- \rightarrow \chi_i^0 \chi_j^0$ is described by three s , t , u channel components of the scattering amplitude, using the follow-

ing notations (the indices a, b label the electron and the i -th neutralino chiralities):

$$A_{ij}^{ab} \equiv \frac{e^2}{s} S_{ij}^{ab} + \frac{e^2}{u} U_{ij}^{ab} + \frac{e^2}{t} T_{ij}^{ab} \quad (1)$$

with the tree-level values for the s -channel

$$S_{ij}^{LL} = \frac{2s_w^2 - 1}{4s_w^2 c_w^2} O_{ij} \quad S_{ij}^{LR} = -\frac{2s_w^2 - 1}{4s_w^2 c_w^2} O_{ij}^* \quad (2)$$

$$S_{ij}^{RL} = \frac{1}{2c_w^2} O_{ij} \quad S_{ij}^{RR} = -\frac{1}{2c_w^2} O_{ij}^* \quad (3)$$

$$O_{ij} = Z_{3i}^{N*} Z_{3j}^N - Z_{4i}^{N*} Z_{4j}^N \quad (4)$$

and for the t, u channels

$$U_{ij}^{LL} = -\frac{1}{4s_w^2 c_w^2} (Z_{1i}^{N*} s_w + Z_{2i}^{N*} c_w)(Z_{1j}^N s_w + Z_{2j}^N c_w) \quad (5)$$

$$U_{ij}^{RR} = -\frac{1}{c_w^2} Z_{1i}^N Z_{1j}^{N*} \quad (6)$$

$$T_{ij}^{LR} = \frac{1}{4s_w^2 c_w^2} (Z_{1j}^{N*} s_w + Z_{2j}^{N*} c_w)(Z_{1i}^N s_w + Z_{2i}^N c_w) \quad (7)$$

$$T_{ij}^{RL} = \frac{1}{c_w^2} Z_{1j}^N Z_{1i}^{N*} \quad (8)$$

The quantities Z_{ij}^N are the elements of the 4×4 mixing matrix, defined in a conventional way [4]. For simplicity, we have neglected in the considered asymptotic region the selectron mass in Eq. (1).

For the purposes of a precision test, it becomes mandatory to compute the following perturbative one-loop expansion of the scattering amplitude. This requires the calculation of a large number of Feynman diagrams. The resulting expressions are valid for any value of the c.m. energy $\sqrt{s} = \sqrt{(p_{e^-} + p_{e^+})^2}$. The full one-loop result has been calculated recently [6]. In this work we propose an alternative approach, valid for values of $\sqrt{s}$ “much” larger than all the SUSY sparticle masses involved in the process. In fact, our strategy should now be made very clear. We assume a previous production of the charginos, of the charged Higgs bosons, and of at least two neutralinos with mass $M_{\chi_1^0}, M_{\chi_2^0}$. Calling M_{SUSY} the heaviest of the real and virtual SUSY particles that appear in the processes, and assuming a “reasonable” limit $M_{\text{SUSY}} \simeq 350\text{--}400$ GeV, we shall choose the value $\sqrt{s} \simeq 1$ TeV value to proceed with our approach. This is due to the fact that, in a previous paper only concerned with the charged Higgs pair production [7], we proved that in such a configuration an asymptotic energy logarithmic expansion of so-called “Sudakov type” was reliable, with the only addition of a constant term to the leading quadratic and next-to-leading linear logarithmic terms. This con-

clusion allows to propose a determination of the SUSY parameters entering the Sudakov logarithms, based on measurements of the slope of the total cross section, in which the (complicated) constant terms cancel.

The approach that we shall follow in this paper, that was already used in the combined chargino-charged Higgs analysis [5], will assume that a similar expansion is valid, with only logarithmic and constant terms. To prove this statement would require a detailed comparison of the complete existing calculation [6] with the assumed asymptotic expansion. This will be the goal of a forthcoming rigorous analysis. For the moment, we shall assume its validity as a working ansatz, and we shall show the main relevant consequences that it will be able to produce.

After this preliminary discussion, we are now ready to write the relevant asymptotic expansion of the scattering amplitude at one-loop, in which we shall only retain the leading quadratic and next-to-leading linear logarithmic terms. For this purpose, we shall use the following formal decomposition the separate $F = S, T$ or U subamplitudes (the Born values are those listed in Eqs. (2)–(8)):

$$F_{ij}^{ab} = F_{ij}^{ab, \text{Born}} + F_{ij}^{ab, \text{Born}} c_a^{\text{in}} + F_{ij}^{ab, \text{fin}} + F_{ij}^{ab, \text{ang}} + F_{ij}^{ab, \text{RG}} \quad (9)$$

In the asymptotic expansion, two different kinds of logarithmic terms appear. The first ones are the standard linear ones of Renormalization Group (RG) origin. They are well known and can be derived in a straightforward way replacing in the Born quantities the various bare couplings with running ones. For sake of completeness, we write the related formulas, noticing that they are only requested for the s -channel (purely Higgsino) component, as:

$$S_{ij}^{LL, \text{RG}} = -\frac{\alpha}{4\pi} \left[\log \frac{s}{M^2} \right] O_{ij} \left(\frac{\tilde{\beta}'_0}{c_w^4} - \frac{\tilde{\beta}_0}{s_w^4} \right) \quad (10)$$

$$S_{ij}^{LR, \text{RG}} = \frac{\alpha}{4\pi} \left[\log \frac{s}{M^2} \right] O_{ij}^* \left(\frac{\tilde{\beta}'_0}{c_w^4} - \frac{\tilde{\beta}_0}{s_w^4} \right) \quad (11)$$

$$S_{ij}^{RL, \text{RG}} = -\frac{\alpha}{\pi} \left[\log \frac{s}{M^2} \right] O_{ij} \left(\frac{\tilde{\beta}'_0}{2c_w^4} \right) \quad (12)$$

$$S_{ij}^{RR, \text{RG}} = \frac{\alpha}{\pi} \left[\log \frac{s}{M^2} \right] O_{ij}^* \left(\frac{\tilde{\beta}'_0}{2c_w^4} \right) \quad (13)$$

where $\tilde{\beta}_0 = -1/4$ and $\tilde{\beta}'_0 = -11/4$. The second type of logarithms which arise asymptotically is that of the “genuine weak” Sudakov terms. These are usually classified [8] as logarithms of gauge nonuniversal, gauge universal, and Yukawa origin. The gauge nonuniversal, scattering angle dependent ones, stem from box diagrams and T, U channel vertices and have the following expressions:

$$S_{ij}^{LL,ang} = -\frac{\alpha}{4\pi s_w^4} \left[\log \frac{s}{M_w^2} \right] \left[\log \frac{-t}{s} [2Z_{2i}^{N*} Z_{2j}^N + Z_{4i}^{N*} Z_{4j}^N] - \log \frac{-u}{s} [2Z_{2j}^N Z_{2i}^{N*} + Z_{3j}^N Z_{3i}^{N*}] \right] \quad (14)$$

$$S_{ij}^{LR,ang} = -\frac{\alpha}{4\pi s_w^4} \left[\log \frac{s}{M_w^2} \right] \left[\log \frac{-t}{s} [2Z_{2i}^N Z_{2j}^{N*} + Z_{3i}^N Z_{3j}^{N*}] - \log \frac{-u}{s} [2Z_{2j}^{N*} Z_{2i}^N + Z_{4j}^{N*} Z_{4i}^N] \right] \quad (15)$$

$$U_{ij}^{LL,ang} = \frac{\alpha}{4\pi s_w^4 c_w} \left[\log \frac{s}{M_w^2} \right] \left\{ \left[Z_{2i}^{N*} (Z_{1j}^N s_w - Z_{2j}^N c_w) + Z_{2j}^N (Z_{1i}^{N*} s_w - Z_{2i}^{N*} c_w) \right] \log \frac{-t}{s} + [Z_{1j}^{N*} s_w + Z_{2j}^N c_w] + Z_{2j}^N (Z_{1i}^{N*} s_w + Z_{2i}^{N*} c_w) \right\} \log \frac{-u}{s} \quad (16)$$

$$T_{ij}^{LR,ang} = -\frac{\alpha}{4\pi s_w^4 c_w} \left[\log \frac{s}{M_w^2} \right] \left\{ [Z_{2j}^{N*} (Z_{1i}^N s_w - Z_{2i}^N c_w) + Z_{2i}^N (Z_{1j}^{N*} s_w - Z_{2j}^{N*} c_w)] \log \frac{-u}{s} + [Z_{2j}^{N*} (Z_{1i}^N s_w + Z_{2i}^N c_w) + Z_{2i}^N (Z_{1j}^{N*} s_w + Z_{2j}^{N*} c_w)] \log \frac{-t}{s} \right\} \quad (17)$$

The gauge universal ones are due both to the initial and to the final vertices. The initial contribution is fixed by the coefficients

$$c_L^{\text{in}} = \frac{\alpha(1 + 2c_w^2)}{16\pi s_w^2 c_w^2} \left[2 \log \frac{s}{M_w^2} - \log^2 \frac{s}{M_w^2} \right] \quad (18)$$

$$c_R^{\text{in}} = \frac{\alpha}{4\pi c_w^2} \left[2 \log \frac{s}{M_w^2} - \log^2 \frac{s}{M_w^2} \right] \quad (19)$$

The contribution from final neutralino legs is different for the s or u , t channels. For the s -channel we have Higgsino components

$$S_{ij}^{ab,fin} = \sum_k \{ S_{ik}^{ab,Born} [c_{kj}^{\text{fin gauge}} + c_{kj}^{\text{fin Yukawa}}] + S_{kj}^{ab,Born} [c_{ki}^{\text{fin gauge}} + c_{ki}^{\text{fin Yukawa}}]^* \} \quad (20)$$

where

$$c_{kj}^{\text{fin gauge}} = \left(\frac{\alpha}{\pi} \right) \frac{(1 + 2c_w^2)}{32s_w^2 c_w^2} \left[2 \log \frac{s}{M_w^2} - \log^2 \frac{s}{M_w^2} \right] [(Z_{4k}^{N*} Z_{4j}^N + Z_{3k}^{N*} Z_{3j}^N) P_L + (Z_{4k}^N Z_{4j}^{N*} + Z_{3k}^N Z_{3j}^{N*}) P_R] \quad (21)$$

The logarithms of Yukawa origin are only due to final s -channel vertices with virtual heavy (b,t) quark-squark pairs. These are the only logarithmic terms that contain (also) the VEVs ratio $\tan\beta$ and their expression is

$$c_{kj}^{\text{fin Yukawa}} = \left(\frac{\alpha}{\pi} \right) \left[-\log \frac{s}{M^2} \right] \left(\frac{3}{16s_w^2 M_w^2} \right) \left[\frac{m_t^2}{\sin^2 \beta} (Z_{4k}^{N*} Z_{4j}^N P_L + Z_{4k}^N Z_{4j}^{N*} P_R) + \frac{m_b^2}{\cos^2 \beta} (Z_{3k}^{N*} Z_{3j}^N P_L + Z_{3k}^N Z_{3j}^{N*} P_R) \right] \quad (22)$$

To conclude, the final contribution to the U and T channel amplitudes is due to gaugino components for which there is no Yukawa contribution:

$$U_{ij}^{ab,fin} = \sum_k \{ U_{ik}^{ab,Born} [c_{kj}^{\text{fin gauge}}] + U_{kj}^{ab,Born} [c_{ki}^{\text{fin gauge}}]^* \} \quad (23)$$

$$T_{ij}^{ab,fin} = \sum_k \{ T_{ik}^{ab,Born} [c_{kj}^{\text{fin gauge}}] + T_{kj}^{ab,Born} [c_{ki}^{\text{fin gauge}}]^* \} \quad (24)$$

with

$$c_{kj}^{\text{fin gauge}} = -\frac{\alpha}{4\pi s_w^2} [Z_{2k}^{N*} Z_{2j}^N P_L + Z_{2k}^N Z_{2j}^{N*} P_R] \times \log^2 \frac{s}{M_V^2} \quad (25)$$

Equations (10)–(25) represent the complete logarithmic contributions at one-loop to the considered process, and are the main original result of this paper. We expect from our previous discussion their reliability for what concerns the calculation of the slope of the total cross section in the 1 TeV range. To perform the latter, one must first compute the expression of the differential cross section that is readily obtained from the above amplitude. After angular integration, one obtains the approximate (to next-to-leading logarithmic order) asymptotic expression of the total cross section. This will be sufficient to determine the effective asymptotic expression of the slope of the cross section, where by definition possible extra “next-to-next-to-leading” (i.e. constant) terms disappear. This expression will only depend on $\tan\beta$ and on the mixing parameters Z_{ij}^N . The latter ones, in turn, can be expressed as functions of the supersymmetric parameters M_1, M_2, μ and $\tan\beta$. Thus, the final form of the slope will depend on these four parameters.

In order to achieve the maximal theoretical information using our approach, we have combined the theoretical expressions of the slope of the neutralino pair total cross section, given in this paper, with those of the chargino and charged Higgs pairs, given in [5]. In practice, we have limited our analysis to the production of the two light observable final states ($\chi_1^0 \chi_2^0, \chi_2^0 \chi_2^0$) for neutralinos, combined with the production of all the three chargino pairs and of the charged Higgs pair. To work in a consistent way, we have chosen as relevant examples for the masses of the produced pairs three sets of values denoted by S_1, S_2 , and S_3 . The first, S_1 , is the Tesla benchmark point RR2

TABLE I. Input parameters and masses of charginos, and lightest neutralinos for the three input sets S_1 , S_2 , and S_3 . The masses are expressed in GeV.

	S_1	S_2	S_3
M_1	78	100	200
M_2	150	200	400
μ	263	200	100
$\tan\beta$	30	30	30
$\chi_1^\pm$	132	149	95
$\chi_2^\pm$	295	266	417
χ_1^0	75	92	82
χ_2^0	133	153	109

[9] with the two lightest neutralinos being, respectively, 95% bino and 82% wino. The set S_2 is a mixed scenario with neutralinos having non negligible gaugino and Higgsino components; χ_1^0 is 86% bino and 13% Higgsino, χ_2^0 is 11% bino, 48% wino and 41% Higgsino. Finally, S_3 is a purely Higgsino one with the two lightest neutralinos being 92% and 98% Higgsino-like. The values of the input parameters as well as the masses of the two charginos and of the two lightest neutralinos are summarized in Table I. We have performed a standard χ^2 analysis assuming in the various scenarios 10–12 experimental points at energies ranging from 700–850 GeV (depending on the scenario) up to 1200 GeV and assuming an experimental accuracy of 1% for the cross sections of gauginos and 2% for that of Higgs bosons. For each scenario we have checked the condition $\sqrt{s} \gg M_{\text{SUSY}}$. The results of our analysis are shown in Figs. 1–3. From inspection of the figures one can draw the following conclusions. In Fig. 1 we consider the S_1 benchmark point. One notices that a combined analysis is able

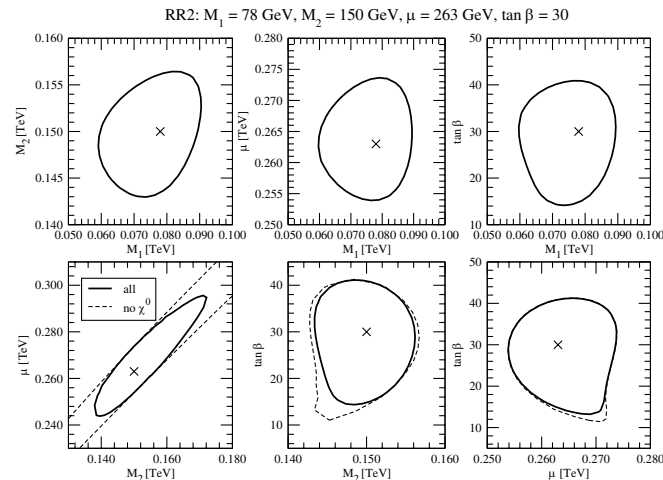


FIG. 1. S_1 benchmark point. 1σ error bounds on the MSSM parameters M_2 , μ , $\tan\beta$. In this and in the following figures the crosses denote the values of the parameters in the specific benchmark.

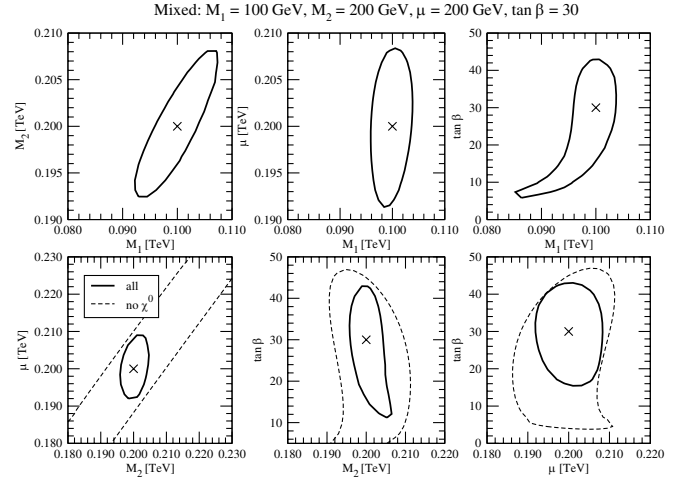


FIG. 2. S_2 benchmark point. 1σ error bounds on the MSSM parameters M_2 , μ , $\tan\beta$.

to generate closed contours in the planes of all possible six couples of parameters. This possibility is obviously existing for the first three cases i.e. (M_1, M_2) , (M_1, μ) , $(M_1, \tan\beta)$ under the condition that the neutralino information is added to the remaining ones, that do not depend on M_1 . Less obvious and more illustrative is the closure of the undetermined strip in the (M_2, μ) plane (drawn in the absence of neutralino data) when neutralino data are added to the remaining ones. This addition does not practically improve, on the contrary, the bounds on $(M_2, \tan\beta)$ and $(\mu, \tan\beta)$ obtained from chargino-Higgs data. One sees typical errors, under the assumed experimental conditions, of about 10 GeV for M_1 , M_2 , μ and of a relative ~ 30 –40% for $\tan\beta$. In Fig. 2 we consider the S_2 scenario. One finds, approximately, the same features for the set of projections. The size of errors is now of approximately ~ 10 GeV for M_1 , M_2 , and μ , a relative

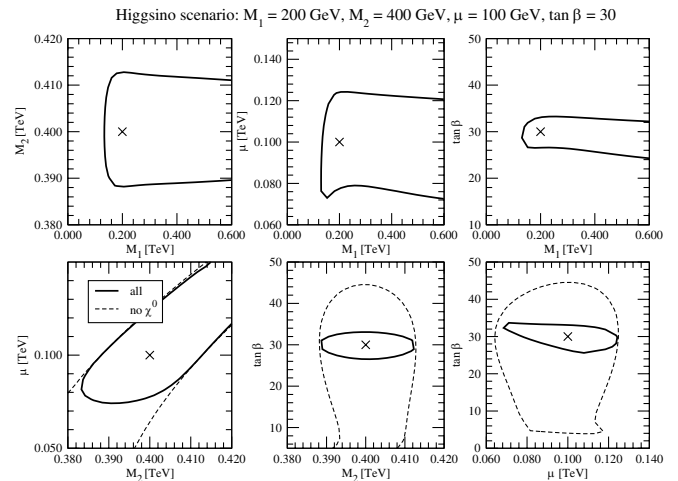


FIG. 3. S_3 scenario. 1σ error bounds on the MSSM parameters M_2 , μ , $\tan\beta$.

40%–50% for $\tan\beta$. Figure 3 describes S_3 , a typical Higgsino scenario. Here the new (negative) feature concerns the lack of boundary for M_1 , as seen from the first three plots. This can be understood since, at the considered M_1 , M_2 and μ values, the mixing parameters Z_{ij}^N do not vary appreciably when M_1 increases. On the contrary, the three plots in the bottom line retain the typical features of the previous cases, with particular relevance of the neutralino role for the determination of lower limits for μ and M_2 . The errors are now, typically, of about 20 GeV for M_2 , μ and of a relative $\sim 10\%$ for $\tan\beta$.

The previous results should illustrate the aimed possible outcomes of the testing strategy that we are proposing in this preliminary qualitative paper. Our assumed

physical inputs will necessarily be the masses of the (supposedly produced) (light) neutralinos, charginos and charged Higgs. Their values will depend on the four parameters M_1 , M_2 , μ , $\tan\beta$ but, in general there will not be a 1-1 correspondence, and different sets of parameters might reproduce “essentially” the same masses [10]. Within the errors that we have illustrated in our examples, these different sets can be discriminated via the χ^2 analysis that we have proposed, and the “correct” set is selected by the true experimental data, if the latter are actually described by the model. If none of the candidate sets were compatible with the analysis, an indication would arise that some of the details of the model might need a suitable modification.

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